Let m be a positive integer. It is given that $2023^k + k$ divides $m^k + k$ for every positive integer k. Show that for all m satisfying the given condition, $m^{2023} - 10$ is divisible by 11.