Problem of the Month - April 2024

In a dance competition with n dancers (where $n > 2$), each dancer performed exactly once
For every pair of dancers, there was a moment when both were dancing simultaneously. Prove
that, at some point, all the dancers were dancing simultaneously.